

# Modeling of an Oil-Free Carbon Dioxide Compressor Using Sanderson-Rocker Arm Motion (S-RAM) Mechanism

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# Learning Objectives

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- Introduction to a CO<sub>2</sub> compressor using a novel driving mechanism
- Introduction to the integrated simulation model

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# Outline

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- Introduction
- Modeling Effort
  - Kinematics model
  - In-cylinder process model
  - Gas pulsation in discharge pipes
  - Overall energy balance model
- Numerical Methodology
- Simulation Results
- Future Work

# Introduction



- High efficiency mechanism to convert shaft rotary motion into piston reciprocating motion.
- Patents  
35+ patents issued since the first patent in 2000

# Introduction



## ➤ Features

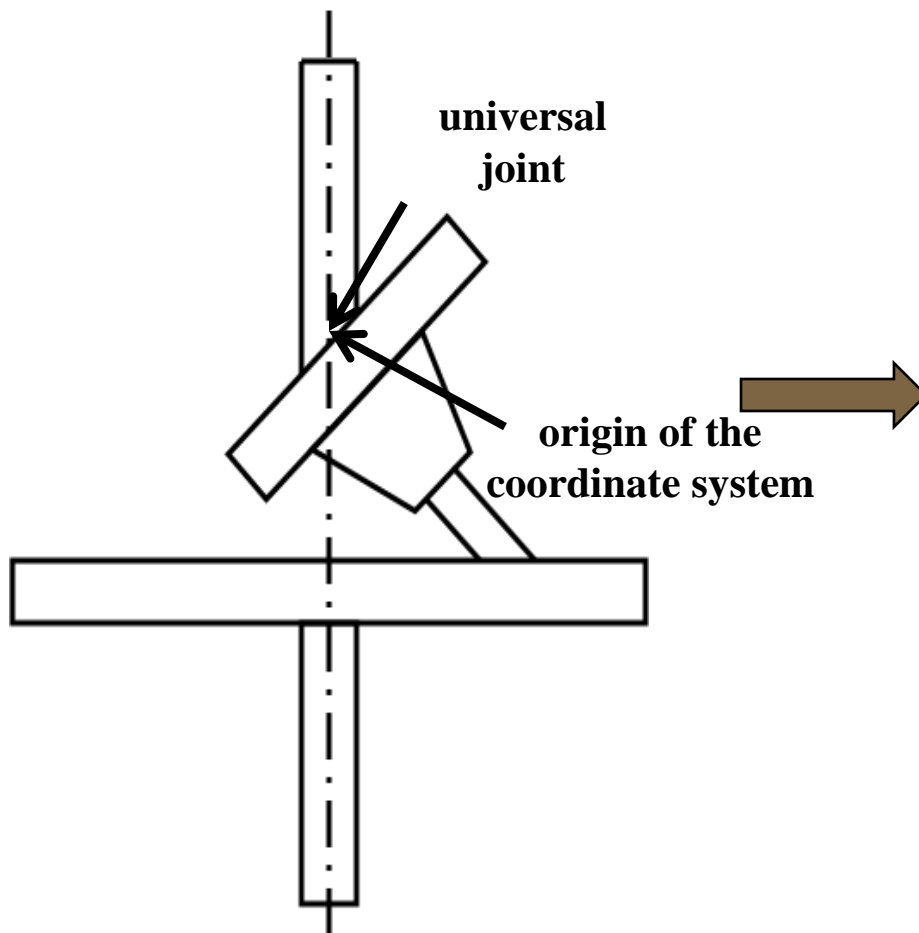
- Oil free
- Less frictional power loss
- Variable capacity control  
(constant clearance volume above the piston top!)

# Outline

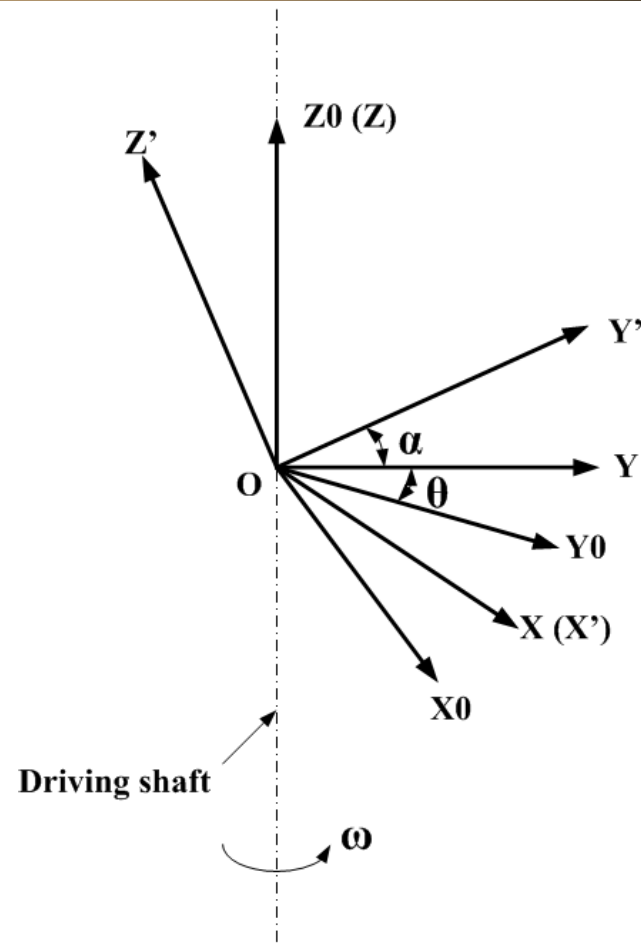
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# Kinematics Model

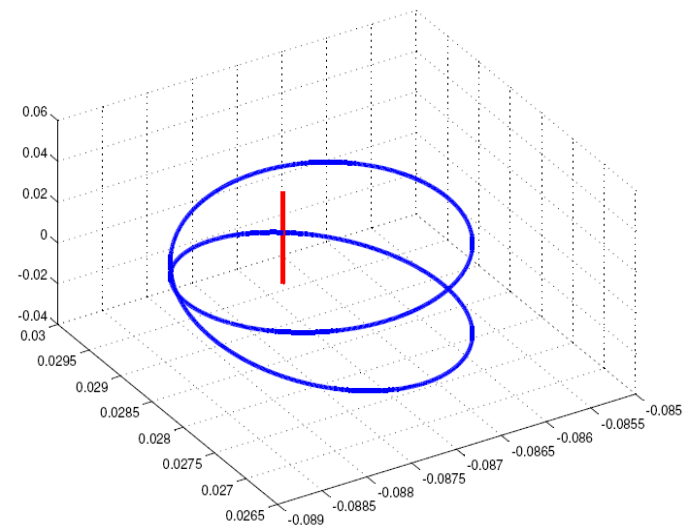
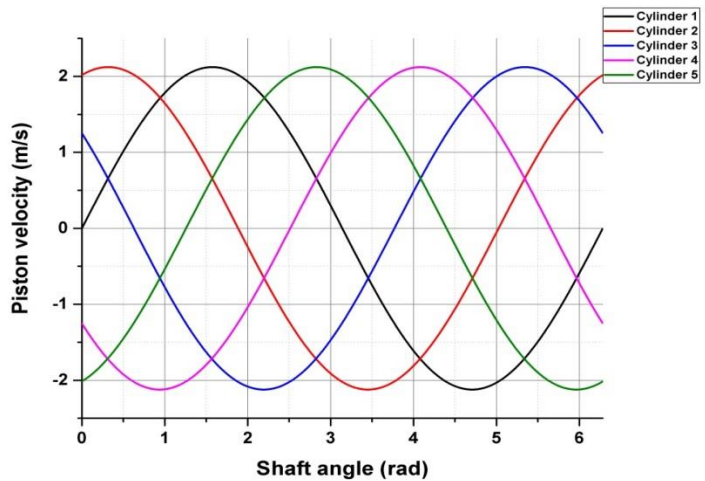
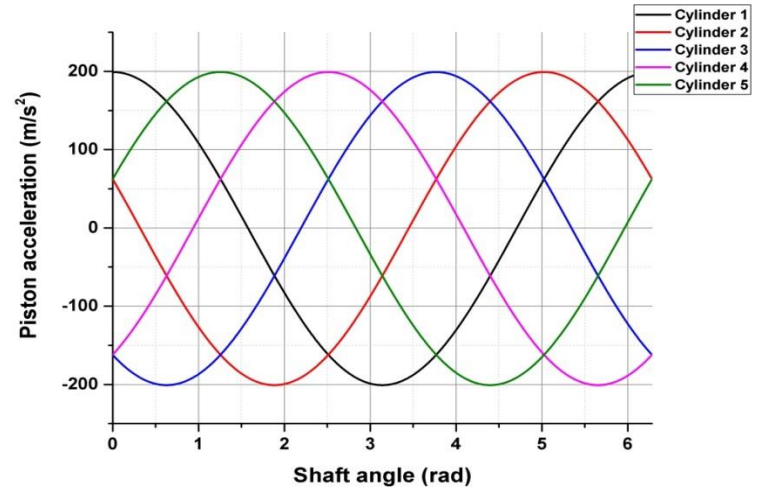
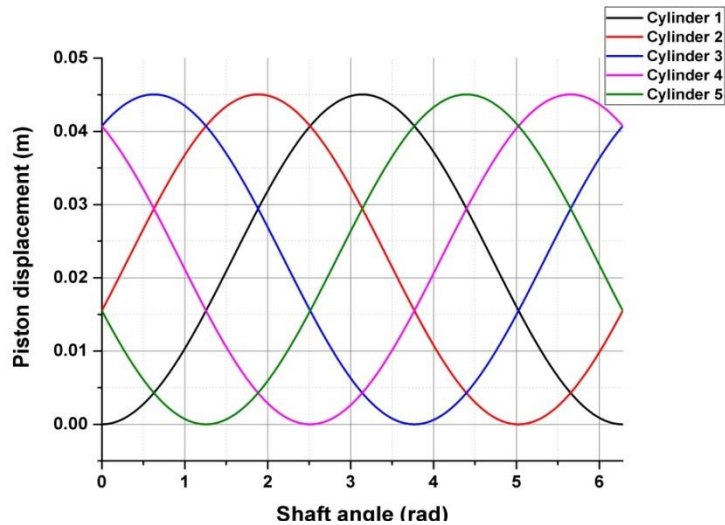


## Schematic of Driving Mechanism



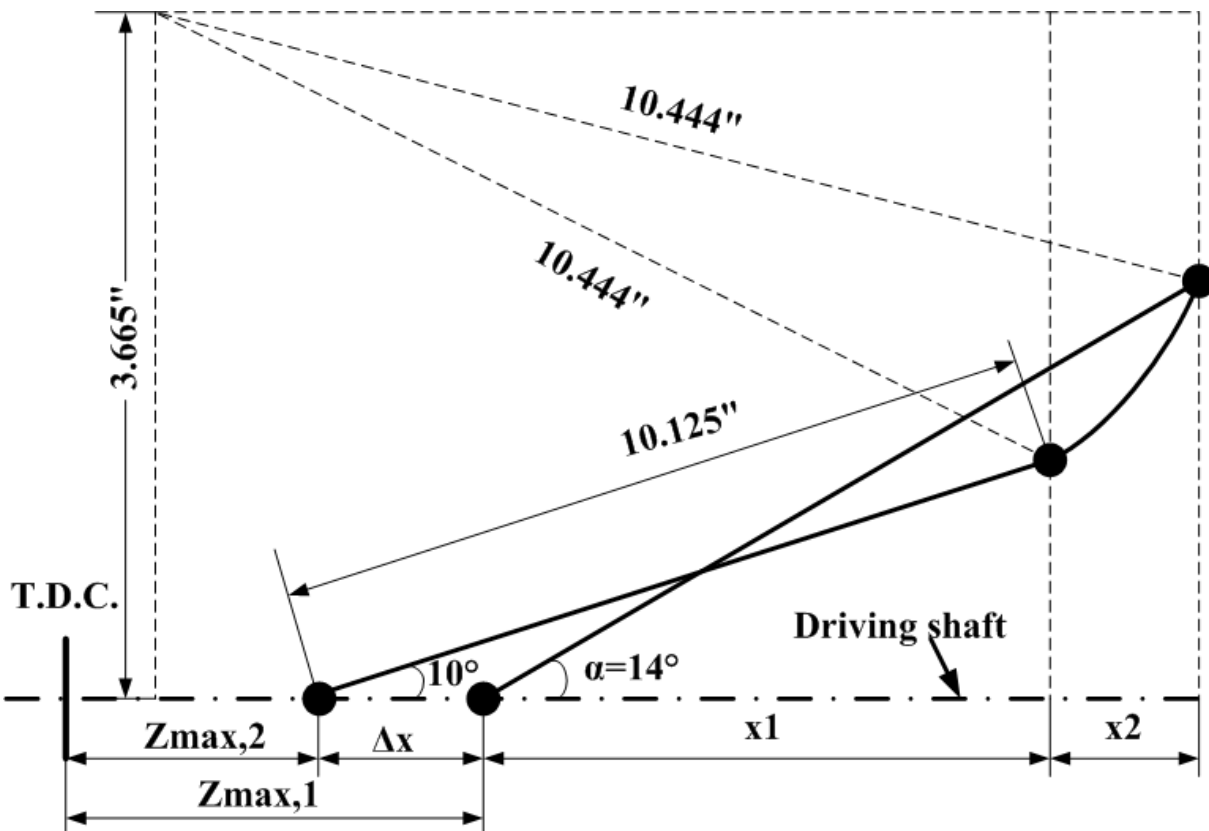
## Coordinate System

# Kinematics Model





# Kinematics Model



$$\alpha = 14^\circ, Z_{\max,1} = 0.044678m$$

$$\alpha = 10^\circ, Z_{\max,2} = 0.0383865m$$

$$Z_{\max,1} = Z_{\max,2} + \Delta x$$

$$\Delta x + x_1 = 10.125 \cdot \cos 10^\circ$$

$$x_1 + x_2 = 10.125 \cdot \cos 14^\circ$$

$$\Delta x = 10.125 \cdot (\cos 10^\circ - \cos 14^\circ) + x_2$$

$$= 0.14693 + 0.10553$$

$$= 0.25246'' = 0.006413m$$

$$Z_{\max,1} = Z_{\max,2} + \Delta x$$

# In-cylinder Process Model

## Governing equations

→ Continuity equation:

$$\frac{dm_c}{dt} = \frac{dm_{suc}}{dt} + \frac{dm_{li}}{dt} - \frac{dm_{dis}}{dt} - \frac{dm_{lo}}{dt}$$

→ Kinematic equation:

$$\frac{dv_c}{dt} = \frac{1}{m_c} \frac{dV_c}{dt} - \frac{V_c}{m_c^2} \frac{dm_c}{dt}$$

→ Energy equation:

$$\frac{dQ}{dt} + \frac{dW}{dt} = \frac{d(m_c u_c)}{dt} + \frac{dm_{dis}}{dt} h_{dis} + \frac{dm_{lo}}{dt} h_{lo} - \frac{dm_{suc}}{dt} h_{suc} - \frac{dm_{li}}{dt} h_{li}$$

Leakage model: isentropic, compressible fluid

$$\left\{ \begin{array}{l} \dot{m}_{gap} = \frac{dm_{gap}}{dt} = C_{gap} A_{gap} p_u \left( \frac{2}{ZRT_u} \right)^{\frac{1}{2}} \left\{ \frac{\kappa}{\kappa-1} \left[ \left( \frac{p_d}{p_u} \right)^{\frac{2}{\kappa}} - \left( \frac{p_d}{p_u} \right)^{\frac{\kappa+1}{\kappa}} \right] \right\}^{\frac{1}{2}}, \frac{p_d}{p_u} > 0.54 \\ \dot{m}_{gap} = \frac{dm_{gap}}{dt} = C_{gap} A_{gap} p_u \left( \frac{\kappa}{ZRT_u} \right)^{\frac{1}{2}} \left[ \left( \frac{2}{\kappa+1} \right)^{\frac{\kappa+1}{\kappa-1}} \right]^{\frac{1}{2}}, \frac{p_d}{p_u} \leq 0.54, \text{choked} \end{array} \right.$$

Valve model: isentropic, compressible fluid

$$\dot{m}_{valve} = \frac{dm_{valve}}{dt} = C_{valve} A_{valve} (2\rho_{high} p_{high})^{\frac{1}{2}} \left\{ \frac{\kappa}{\kappa-1} \left[ \left( \frac{p_{low}}{p_{high}} \right)^{\frac{2}{\kappa}} - \left( \frac{p_{low}}{p_{high}} \right)^{\frac{\kappa+1}{\kappa}} \right] \right\}^{\frac{1}{2}}$$

# Gas Pulsation in Discharge Pipes

- Anechoic assumption
- Elson and Soedel's method (1974)

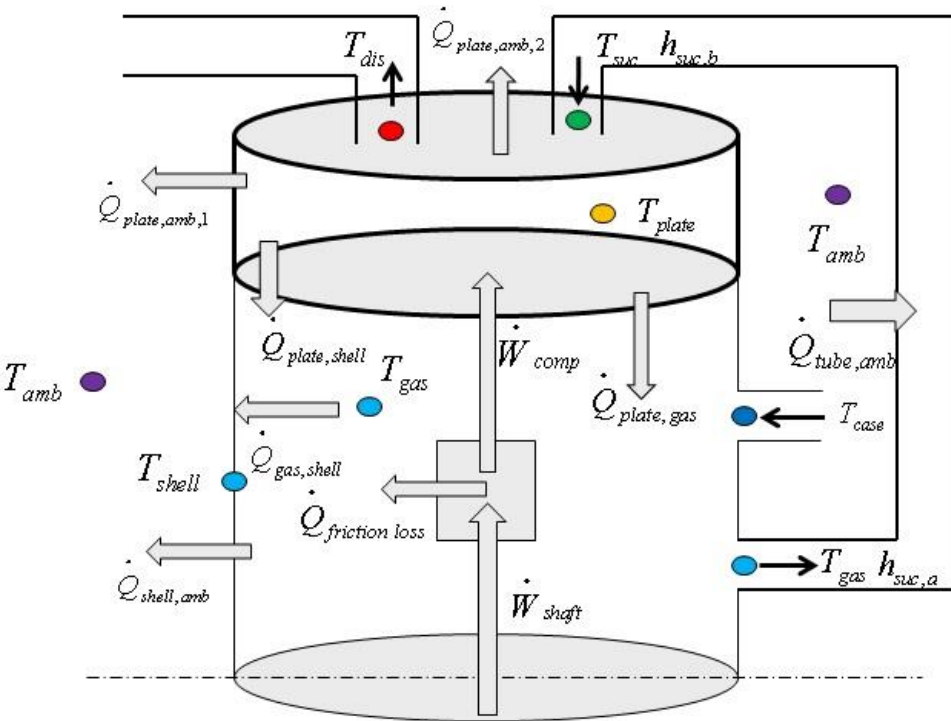
The diagram shows the equation for acoustic impedance  $Z$  with red text labels and blue arrows pointing to the variables:

$$Z = \frac{p_{pul}}{u_{pul}} = \rho_0 c$$

Labels and arrows:

- impedance** (red text) points to  $Z$ .
- oscillated acoustic pressure** (red text) points to  $p_{pul}$ .
- gas velocity** (red text) points to  $u_{pul}$ .
- gas density in the pipeline** (red text) points to  $\rho_0$ .
- speed of sound** (red text) points to  $c$ .

# Overall Energy Balance Model



Schematic of overall energy flow

$$\dot{m}_{comp} (h_{suc,a} - h_{suc,b}) = \dot{Q}_{plate,gas} - \dot{Q}_{gas,shell} + \dot{Q}_{friction,loss}$$

$$\dot{Q}_{gas,shell} - \dot{Q}_{shell,amb} = 0$$

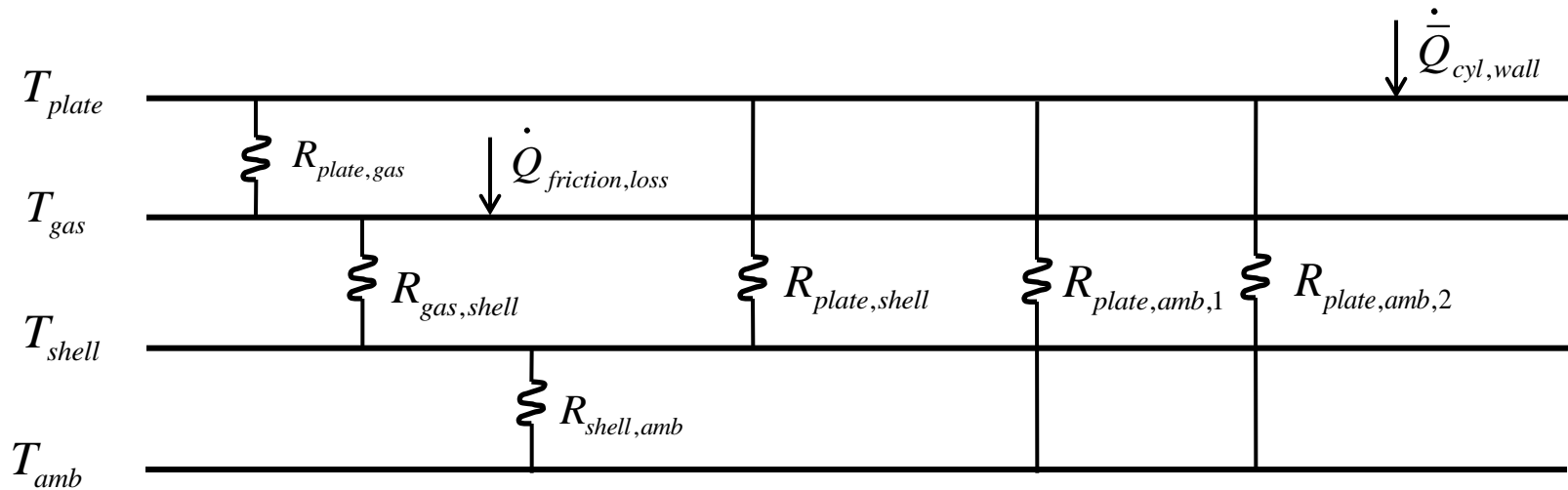
$$-\dot{Q}_{plate,amb,1} - \dot{Q}_{plate,amb,2} - \dot{Q}_{plate,gas} - \dot{Q}_{cyl,wall} = 0$$

$$\dot{Q}_{pipe,amb} + \dot{m}_{comp} (h_{suc,a} - h_{suc,b}) = 0$$

$$\dot{W}_{comp} + \dot{Q}_{cyl,wall} = \dot{m}_{comp} (h_{dis} - h_{suc,b})$$

$$\dot{Q} = \frac{T_a - T_b}{R_{ab}}$$

# Overall Energy Balance Model



**Thermal resistance network of the overall energy balance**

$$\dot{\bar{Q}}_{cyl,wall} = \frac{n}{60} \int_t^{t+\Delta T} \dot{Q}_{cyl,wall} dt$$

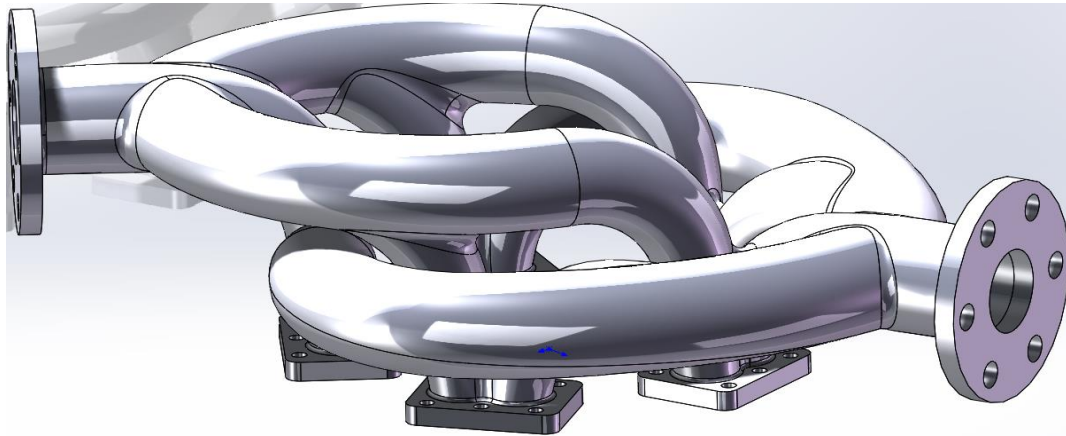
# Overall Energy Balance Model

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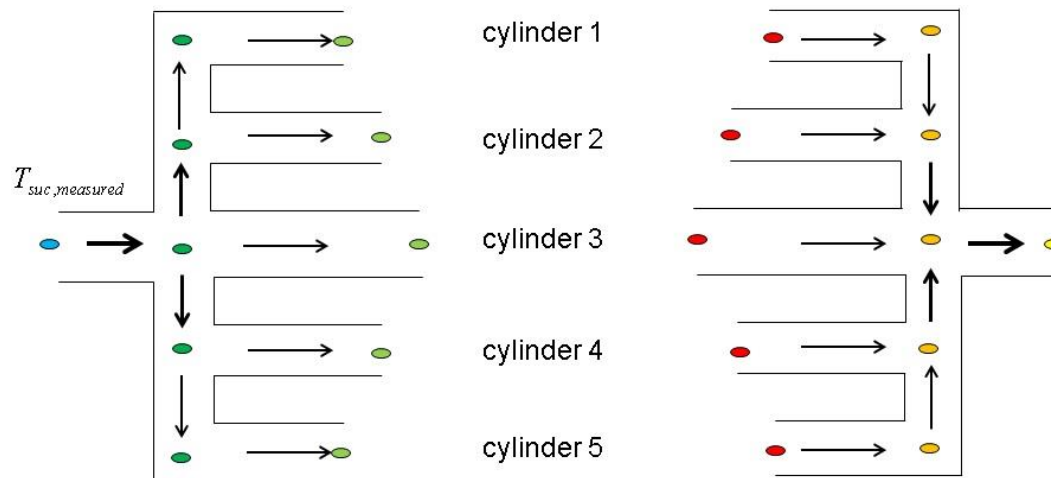
➤ Heat transfer categories:

- Convection along the horizontal plate
- Convection along the vertical plate
- Convection along the horizontal pipe
- Convection along the vertical pipe
- Heat conduction between cylinder plate and case shell  
(neglected here)

# Overall Energy Balance Model



**Real pipe arrangement**



**Simplified pipe arrangement**

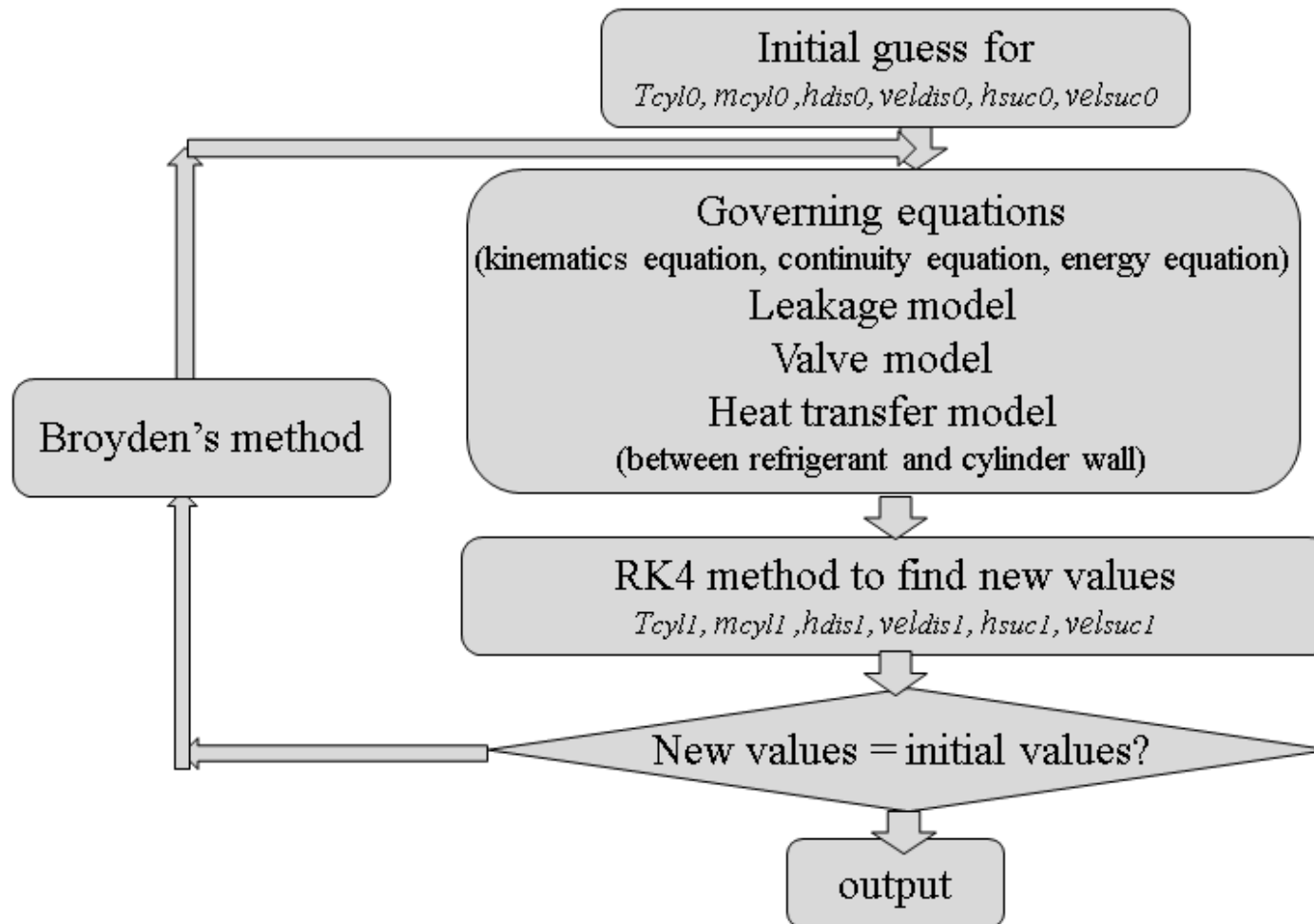
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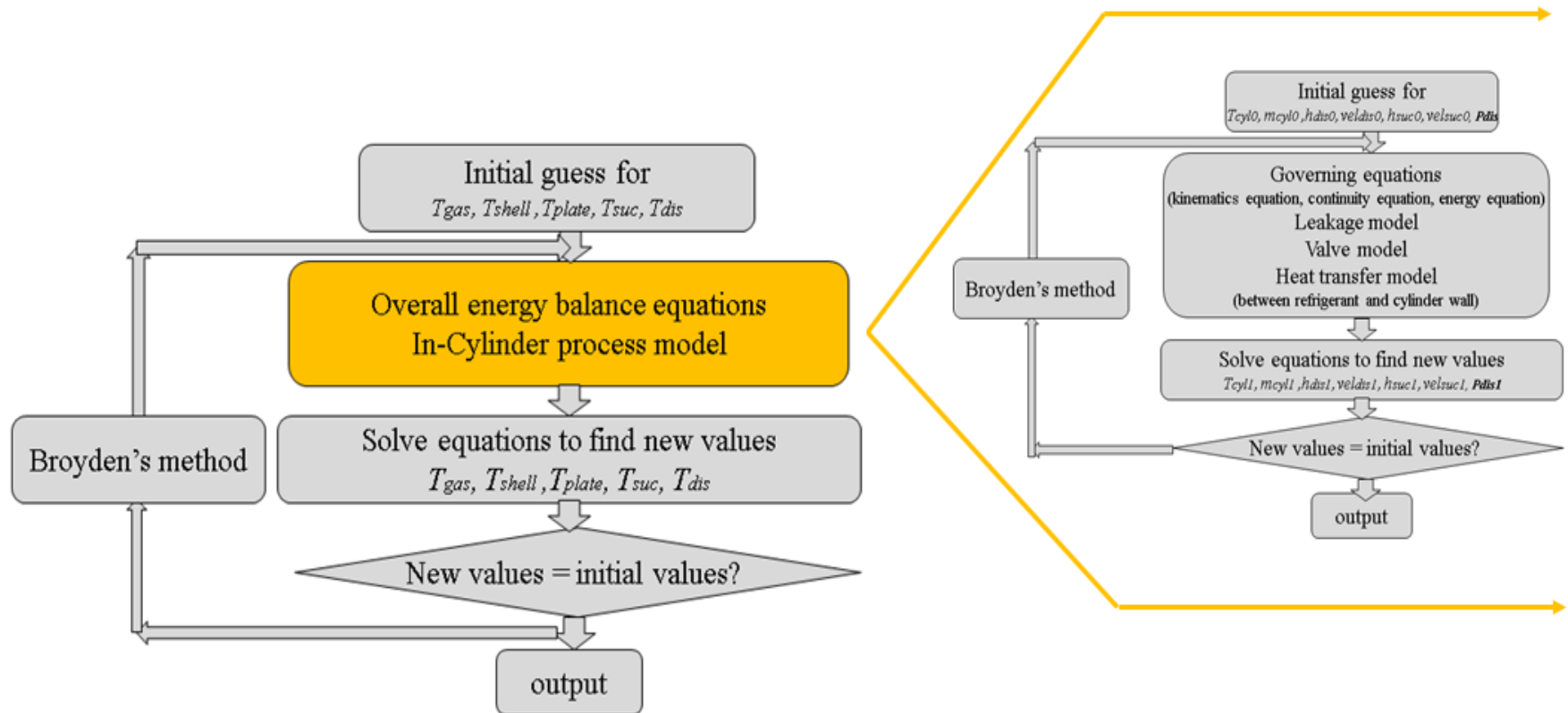


# Numerical Methodology



**Flow chart of in-cylinder process model solution**

# Numerical Methodology



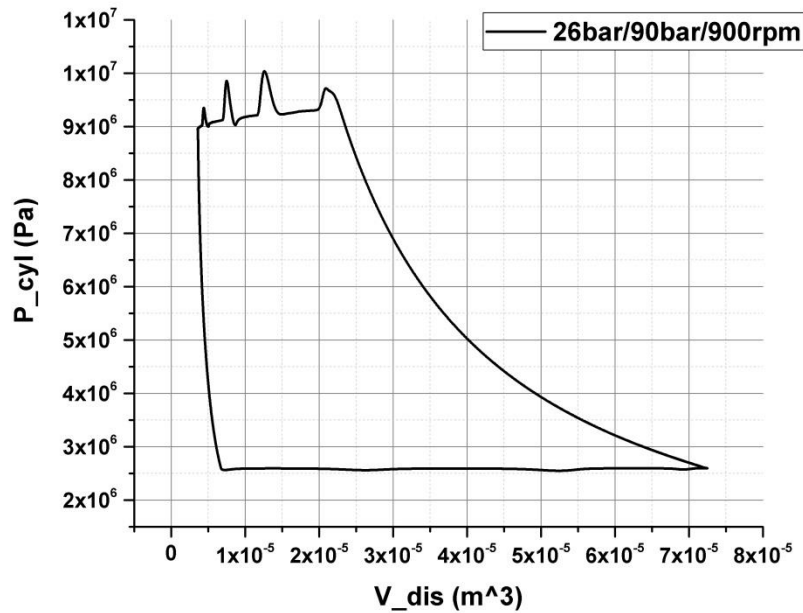
**Flow chart of overall compressor model solution**

# Outline

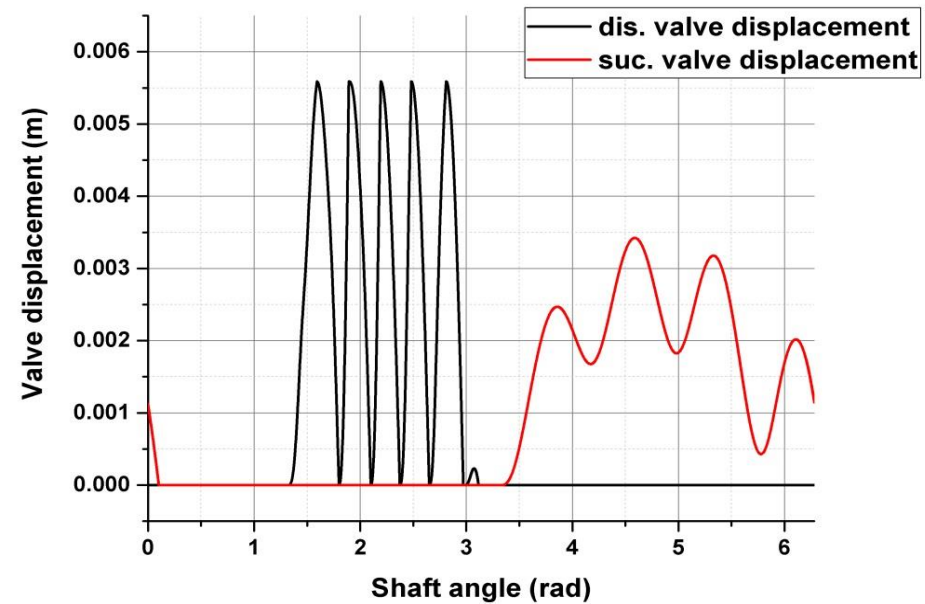
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- **Simulation Results**
- Future Work

# Simulation Results



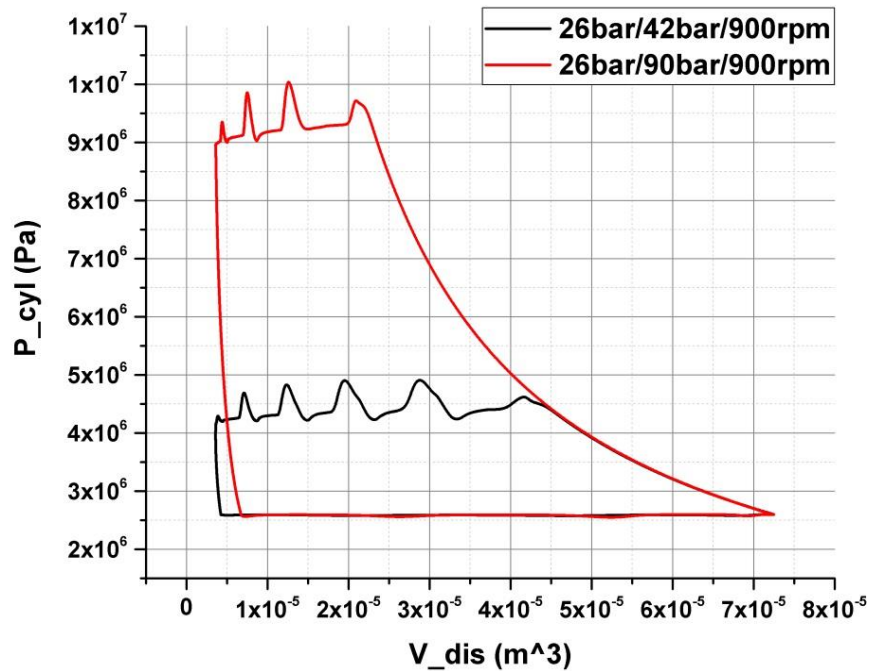
P-V diagram



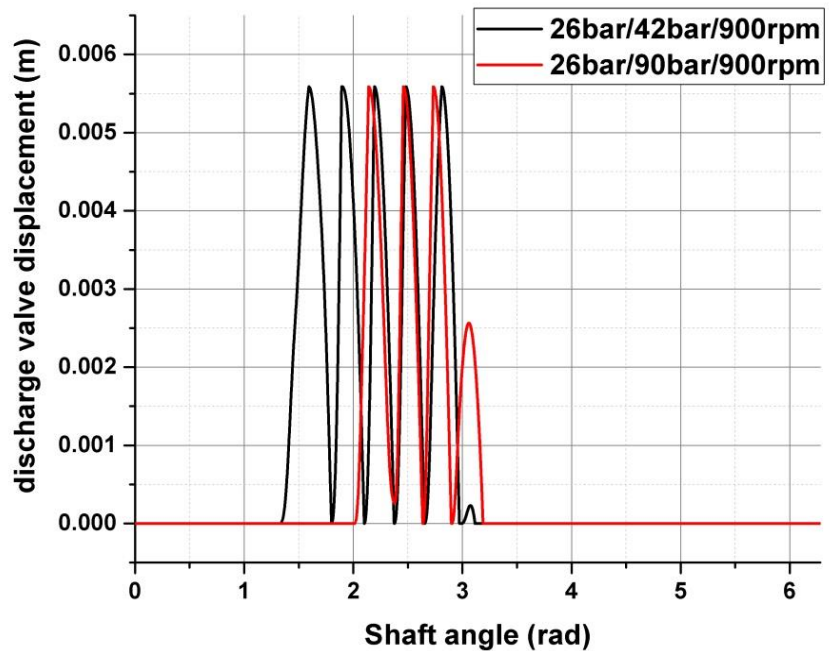
Valve displacement

# Simulation Results

## ➤ Effect of discharge pressure



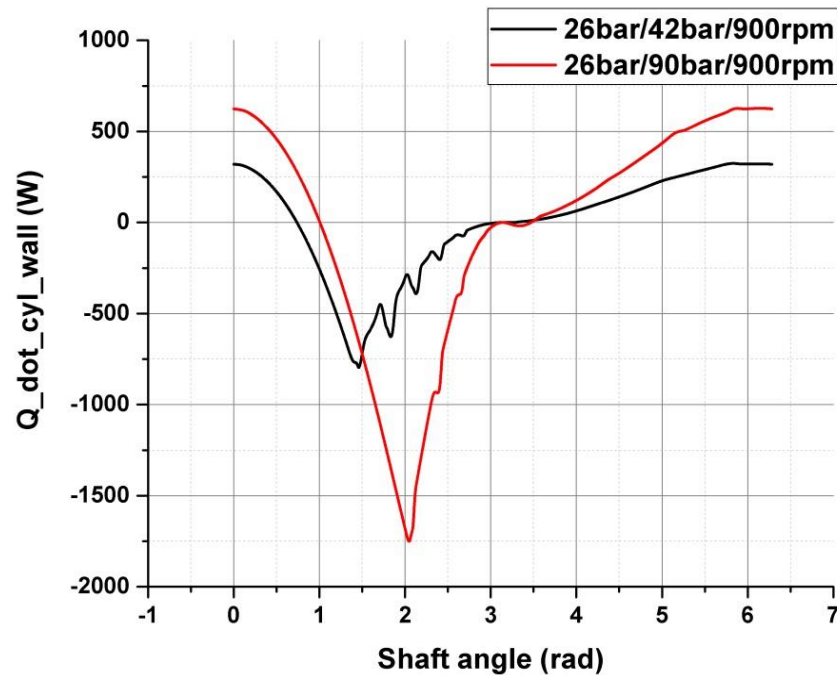
P-V diagram



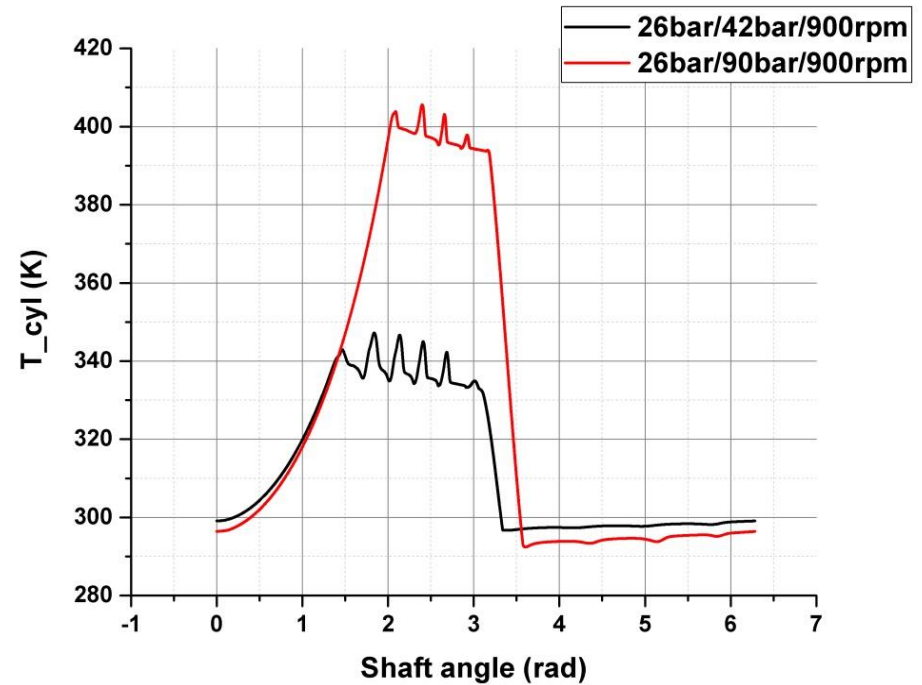
Discharge valve displacement

# Simulation Results

## ➤ Effect of discharge pressure



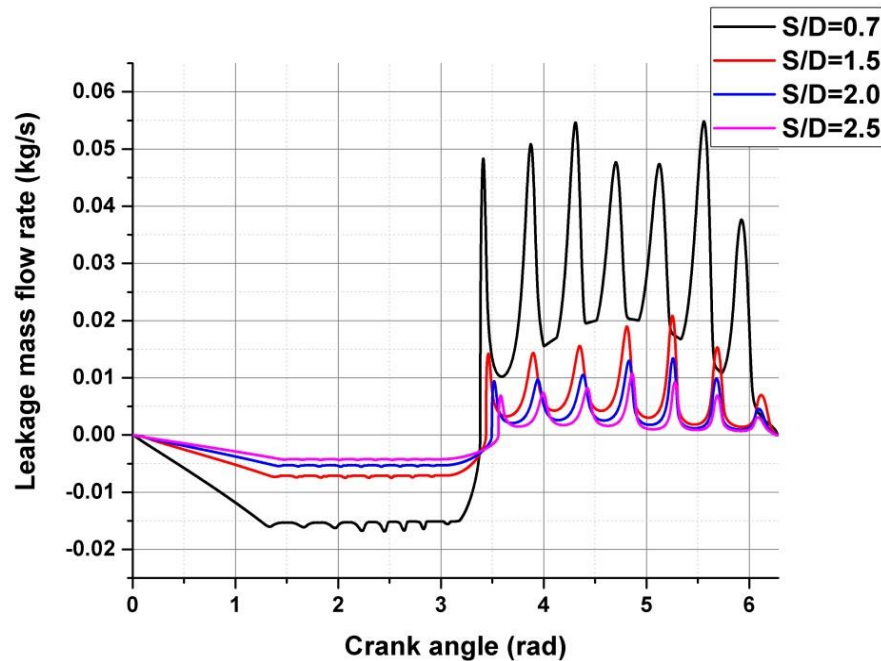
**Instantaneous heat transfer between in-cylinder refrigerant and cylinder wall**



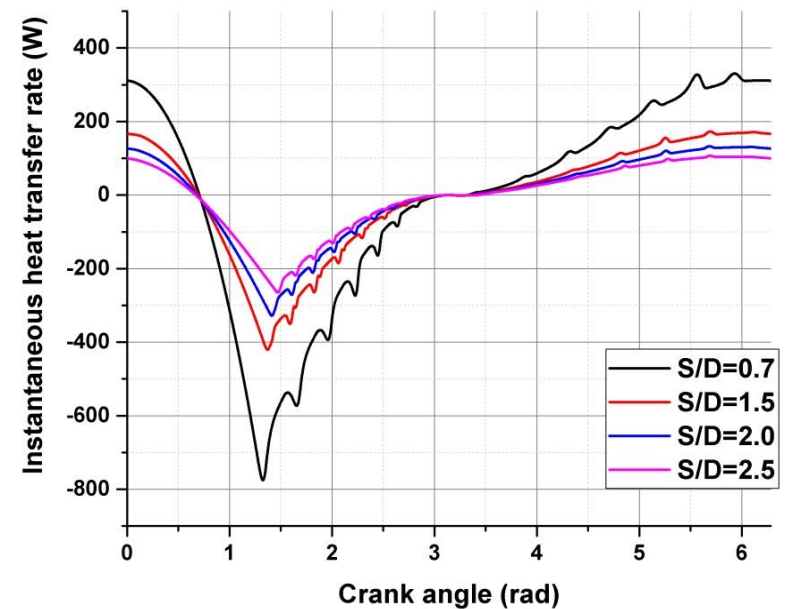
**In-cylinder refrigerant temperature**

# Simulation Results

## ➤ Effect of stroke-to-bore ratio



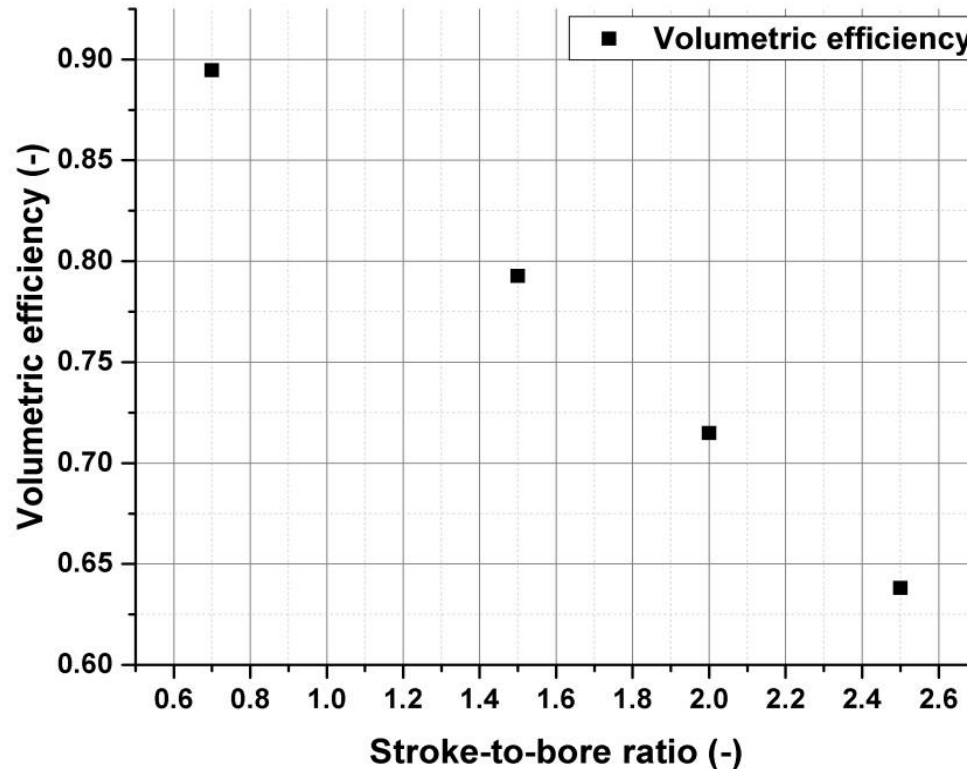
**Instantaneous refrigerant leakage through clearance  
between piston assembly and cylinder wall**



**Instantaneous heat transfer between in-cylinder  
refrigerant and cylinder wall**

# Simulation Results

## ➤ Effect of stroke-to-bore ratio



Effect of stroke-to-bore ratio on the volumetric efficiency



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# Future Work

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- Dynamics model (frictional power loss)
- Performance testing of the prototype compressor
- Discharge pipe gas pulsation measurement
- Validation of the simulation model
- Parametric studies

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# Questions?

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